

## YUKI Algorithm test functions and images

$f_1(x) = f(x_1, x_2, \dots, x_n) = \sum_{i=1}^n x_i^2$	Sphere	[-5.12 5.12]	30
$f_2(x) = f(x_1, \dots, x_n) = \sum_{i=1}^n ix_i^2$	Powell Sum	[-1 1]	30
$f_3(x) = x_1 + d(\sum_{i=2}^n x_i^2)^\alpha$	Powell Sum	[-5 5]	30
$f_4(x) = \sum_{i=1}^{29} (x_i^2)^{(x_{i+1}^2+1)} + (x_{i+1}^2)^{(x_i^2+1)}$	Brown	[-4 4]	30
$f_5(x) = f(x_1, \dots, x_{30}) = -\exp(-0.5 \sum_{i=1}^{30} x_i^2)$	Exponential	[-2 2]	30
$f_6(x) = f(x_1, \dots, x_{30}) = \exp(-\sum_{i=1}^{30} (x_i/15)^{10}) - 2\exp(-\sum_{i=1}^{30} x_i^2) \prod_{i=1}^{30} \cos^2(x_i)$	Xin-She Yang N. 3	[-10 10]	30
$f_7(x) = f_7(x_1, \dots, x_{30}) = \sum_{i=1}^{30} x_i^2 + (\sum_{i=1}^{30} 0.5ix_i)^2 + (\sum_{i=1}^{30} 0.5ix_i)^4$	Zakharov	[-10 10]	30
$f_8(x) = f(x_1, \dots, x_{30}) = \sum_{i=1}^{30}  x_i $	Schwefel 2.20	[-100 100]	30
$f_9(x) = f(x_1, \dots, x_{30}) = \max_{i=1, \dots, 30}  x_i $	Schwefel 2.21	[-100 100]	30
$f_{10}(x) = f(x_1, \dots, x_{30}) = \sum_{i=1}^{30}  x_i  + \prod_{i=1}^{30}  x_i $	Schwefel 2.22	[-10 10]	30

$f_{11}(x) = f_{11}(x_1, \dots, x_{30}) = \sum_{i=1}^{29} [100(x_{i+1} - x_i^2)^2 + (x_i - 1)^2]$	Rosenbrock	[-30 30]	30
$f_{12}(x) = f_{12}(x_1, x_2, \dots, x_{30}) = \sum_{i=1}^{30} -x_i \sin(\sqrt{ x_i })$	Schwefel	[-500 500]	30
$f_{13}(x) = f_{13}(x_1, x_2, \dots, x_{30}) = \sum_{i=1}^{30} [x_i^2 - 10 \cos(2\pi x_i) + 10]$	Rastrigin	[-5.12 5.12]	30
$f_{14}(x) = f(x_1, \dots, x_{30}) = (\sum_{i=1}^{30}  x_i ) \exp(-\sum_{i=1}^{30} \sin(x_i^2))$	Xin-She Yang N. 2	[-6.28 6.28]	30
$f_{15}(x) = f(x_1, \dots, x_{30}) = (\sum_{i=1}^{30} \sin^2(x_i) - e^{-\sum_{i=1}^{30} x_i^2}) e^{-\sum_{i=1}^{30} \sin^2 \sqrt{ x_i }}$	Xin-She Yang N. 4	[-10 10]	30
$f_{16}(x) = [(\ \mathbf{x}\ ^2 - 30)^2]^\alpha + \frac{1}{n} (\frac{1}{2} \ \mathbf{x}\ ^2 + \sum_{i=1}^{30} x_i) + \frac{1}{2}$	Happy Cat	[-2 2]	30
$f_{17}(x) = f(x_1 \dots x_{30}) = 1 + \sum_{i=1}^{30} \sin^2(x_i) - 0.1 e^{\sum_{i=1}^{30} x_i^2}$	Periodic	[-10 10]	30
$f_{18}(x) = f(x_1, \dots, x_{30}) = \sum_{i=1}^{30} ix_i^4 + \text{random}[0,1]$	Quartic	[-1.28 1.28]	30

$f_{19}(x) = f(x_1, \dots, x_{30}) = \sum_{i=1}^{30} \sum_{j=1}^5 j \sin((j+1)x_i + j)$	Shubert 3	[-10 10]	30
$f_{20}(x) = f(x_1, \dots, x_{30}) = 1 - \cos(2\pi \sqrt{\sum_{i=1}^D x_i^2}) + 0.1 \sqrt{\sum_{i=1}^D x_i^2}$	Salomon	[-4 4]	30

$f_{21}(x, y) = 2x^2 - 1.05x^4 + \frac{x^6}{6} + xy + y^2$	Three-Hump Camel	[-2 2]	2
$f_{22}(x, y) = -\frac{1 + \cos(12\sqrt{x^2 + y^2})}{(0.5(x^2 + y^2) + 2)}$	Drop-Wave	[-5 5]	2
$f_{23}(x, y) = 100(y - x^3)^2 + (1 - x)^2$	Leon	[-2 2]	2
$f_{24}(x, y) = (x + 2y - 7)^2 + (2x + y - 5)^2$	Booth	[-10 10]	2
$f_{25}(x, y) = 0.26(x^2 + y^2) - 0.48xy$	Matyas	[-10 10]	2
$f_{26}(x, y) = (x + 10)^2 + (y + 10)^2 + e^{-x^2 - y^2}$	Brent	[-20 0]	2
$f_{27}(x, y) = 0.5 + \frac{\sin^2(x^2 + y^2) - 0.5}{(1 + 0.001(x^2 + y^2))^2}$	Schaffer N. 1	[-50 50]	2
$f_{28}(x, y) = -200e^{-0.2\sqrt{x^2 + y^2}}$	Ackley N. 2	[-30 30]	2
$f_{29}(x, y) = x^2 + 2y^2 - 0.3\cos(3\pi x) - 0.4\cos(4\pi y) + 0.7$	Bohachevsky n N. 1	[-100 100]	2
$f_{30}(x, y) = 0.5 + \frac{\cos^2(\sin( x^2 - y^2 )) - 0.5}{(1 + 0.001(x^2 + y^2))^2}$	Schaffer N. 4	[-100 100]	2

$f_{31}(x, y) = -\frac{\sin^2(x - y)\sin^2(x + y)}{\sqrt{x^2 + y^2}}$	Keane	[-10 10]	2
$f_{32}(x, y) = \sin^2(3\pi x) + (x - 1)^2(1 + \sin^2(3\pi y)) + (y - 1)^2(1 + \sin^2(2\pi y))$	Levi N. 13	[-10 10]	2
$f_{33}(x, y) = 100\sqrt{ y - 0.01x^2 } + 0.01 x + 10 $	Bukin N. 6	[-15 5]	2
$f_{34}(x, y) = - \sin(x)\cos(y)\exp( 1 - \frac{\sqrt{x^2 + y^2}}{\pi} ) $	Holder-Table	[-10 10]	2
$f_{35}(x, y) = -0.0001( \sin(x)\sin(y)\exp( 100 - \frac{\sqrt{x^2 + y^2}}{\pi} )  + 1)^{0.1}$	Cross-in-Tray	[-10 10]	2
$f_{36}(x, y, z) = \frac{4}{3}(x^2 + y^2 - xy)^{0.75} + z$	Wolfe	[0 2]	2
$f_{37}(x, y) = x^2 + y^2 + 25(\sin^2(x) + \sin^2(y))$	Egg Crate	[-20 20]	2
$f_{38}(x, y) = \sin(x + y) + (x - y)^2 - 1.5x + 2.5y + 1$	McCormick	[-1.5 4]	2
$f_{39}(x, y) = 10^5 x^2 + y^2 - (x^2 + y^2)^2 + 10^{-5}(x^2 + y^2)^4$	Deckkers-Aarts	[-20 20]	2
$f_{40}(x, y) =  x^2 + y^2 + xy  +  \sin(x)  +  \cos(y) $	Bartels Conn	[-500 500]	2

$f_{41} = 1e - 3 \left( \left\{ \begin{array}{l} f_1 = \textit{Sphere Function} \\ f_2 = \textit{Griewank Function} \\ f_3 = \textit{Griewank Function} \end{array} \right\} \right)$ <p style="text-align: center;"> bias = [100,100,200 ]  <math>\sigma</math> = [10,20,10]  <math>\lambda</math> = [ 0.2,1,0.1] </p>	[-5 5]	2
$f_{42} = 1e - 3 \left( \left\{ \begin{array}{l} f_1 = \textit{Ackley Function} \\ f_2 = \textit{Weierstrass Function} \\ f_3 = \textit{FEF8F2 Function} \end{array} \right\} \right)$ <p style="text-align: center;"> bias = [0,100,200 ]  <math>\sigma</math> = [10,30,10]  <math>\lambda</math> = [1,10,20] </p>	[-5 5]	2
$f_{43} = e - 3 \left( \left\{ \begin{array}{l} f_1 = \textit{Sphere Function} \\ f_2 = \textit{Griewank Function} \\ f_3 = \textit{Griewank Function} \\ f_4 = \textit{Ackley Function} \end{array} \right\} \right)$ <p style="text-align: center;"> bias = [100,200,200,100 ]  <math>\sigma</math> = [10,10,10,10]  <math>\lambda</math> = [ 0.5,1,0.2,0.5] </p>	[-5 5]	2
$f_{44} = e - 4 \left( \left\{ \begin{array}{l} f_1 = \textit{FEF8F2 Function} \\ f_2 = \textit{FEF8F2 Function} \\ f_3 = \textit{Weierstrass Function} \\ f_4 = \textit{Weierstrass Function} \end{array} \right\} \right)$ <p style="text-align: center;"> bias = [100,200,200,100 ]  <math>\sigma</math> = [10,20,40,20]  <math>\lambda</math> = [ 0.1,10,20,20] </p>	[-5 5]	2
$f_{45} = e - 3 \left( \left\{ \begin{array}{l} f_1 = \textit{Griewank Function} \\ f_2 = \textit{Griewank Function} \\ f_3 = \textit{Weierstrass Function} \\ f_4 = \textit{Weierstrass Function} \\ f_5 = \textit{Sphere Function} \\ f_6 = \textit{Sphere Function} \end{array} \right\} \right)$ <p style="text-align: center;"> bias = [0,100,200,300,200,300 ]  <math>\sigma</math> = [40,20,30,40,10,10]  <math>\lambda</math> = [ 1,0.5,2,2,0.1,0.1] </p>	[-5 5]	2

$f_{46} = e - 3 \left( \begin{array}{l} f_1 = \text{FEF8F2 Function} \\ f_2 = \text{FEF8F2 Function} \\ f_3 = \text{Weierstrass Function} \\ f_4 = \text{Weierstrass Function} \\ f_5 = \text{Griewank Function} \\ f_6 = \text{Griewank Function} \end{array} \right)$ <p style="text-align: center;"> bias = [0,100,200,300,200,300 ]  <math>\sigma = [1,1,2,10,10,20]</math>  <math>\lambda = [0.25,0.1,2,1,2,5]</math> </p>	[-5 5]	2
$f_{47} = e - 3 \left( \begin{array}{l} f_1 = \text{Rastrigin Function} \\ f_2 = \text{Rastrigin Function} \\ f_3 = \text{Griewank Function} \\ f_4 = \text{Griewank Function} \\ f_5 = \text{Sphere Function} \\ f_6 = \text{Sphere Function} \\ f_7 = \text{Weierstrass Function} \\ f_8 = \text{Weierstrass Function} \end{array} \right)$ <p style="text-align: center;"> bias = [0,100,200,300,200,300,200,100 ]  <math>\sigma = [20,20,10,10,10,10,20,20]</math>  <math>\lambda = [0.2,0.9,0.2,0.9,0.2,0.2,0.9,0.9]</math> </p>	[-5 5]	2
$f_{48} = e - 3 \left( \begin{array}{l} f_1 = \text{Rastrigin Function} \\ f_2 = \text{Rastrigin Function} \\ f_3 = \text{FEF8F2 Function} \\ f_4 = \text{FEF8F2 Function} \\ f_5 = \text{Weierstrass Function} \\ f_6 = \text{Weierstrass Function} \\ f_7 = \text{Griewank Function} \\ f_8 = \text{Griewank Function} \end{array} \right)$ <p style="text-align: center;"> bias = [0,100,200,200,200,500,500,100 ]  <math>\sigma = [20,20,10,10,10,10,20,20]</math>  <math>\lambda = [0.9,0.9,0.5,0.5,0.5,0.5,0.9,0.9]</math> </p>	[-5 5]	2

$f_{49} = e - 3 \left\{ \begin{array}{l} f_1 = \text{Rastrigin Function} \\ f_2 = \text{Rastrigin Function} \\ f_3 = \text{Weierstrass Function} \\ f_4 = \text{Weierstrass Function} \\ f_5 = \text{Griewank Function} \\ f_6 = \text{Griewank Function} \\ f_7 = \text{Ackley Function} \\ f_8 = \text{Ackley Function} \\ f_9 = \text{Sphere Function} \\ f_{10} = \text{Shere Function} \end{array} \right\}$ <p> bias = [0,100,200,300,200,300,300,400,400,500 ]  <math>\sigma = [1,1,1,10,10,2,20,20,10,2]</math>  <math>\lambda = [1,1,10,10,0.2,0.2,0.5,0.5,0.1,0.1]</math> </p>	[-5 5]	2
$f_{50} = e - 18 \left\{ \begin{array}{l} f_1 = \text{FEF8F2 Function} \\ f_2 = \text{FEF8F2 Function} \\ f_3 = \text{Sphere Function} \\ f_4 = \text{Sphere Function} \\ f_5 = \text{Griewank Function} \\ f_6 = \text{Griewank Function} \\ f_7 = \text{Ackley Function} \\ f_8 = \text{Ackley Function} \\ f_9 = \text{Weierstrass Function} \\ f_{10} = \text{Weierstrass Function} \end{array} \right\}$ <p> bias = [0,100,200,300,200,300,300,100,100,100 ]  <math>\sigma = [1,1,1,2,2,2,1,2,2,1]</math>  <math>\lambda = [0.2,0.5,0.1,0.5,0.5,0.1,0.5,0.5,0.2,0.2]</math> </p>	[-5 5]	2





